Single-Mode Parametric-Down-Conversion States with 50 Photons as a Source for Mesoscopic Quantum Optics

Georg Harder,1,* Tim J. Bartley,1,2 Adriana E. Lita,2 Sae Woo Nam,2 Thomas Gerrits,2 and Christine Silberhorn1
1Integrated Quantum Optics Group, Applied Physics, University of Paderborn, 33098 Paderborn, Germany
2National Institute of Standards and Technology, 325 Broadway, Boulder, Colorado 80305, USA
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We generate pulsed, two-mode squeezed states in a single spatiotemporal mode with mean photon numbers up to 20. We directly measure photon-number correlations between the two modes with transition edge sensors up to 80 photons per mode. This corresponds roughly to a state dimensionality of 6400. We achieve detection efficiencies of 64% in the technologically crucial telecom regime and demonstrate the high quality of our measurements by heralded nonclassical distributions up to 50 photons per pulse and calculated correlation functions up to 40th order.

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Introduction.—The quest to study quantum effects for macroscopic system sizes is driven by one of the most fundamental issues of quantum physics, as exemplified by Schrödinger’s cat states [1], and has initiated much research over the past decades [2–5]. However, the nature of quantum decoherence renders the observation of nonclassical features in large systems increasingly difficult. Optical states are a good candidate to observe nonclassical features and to harness large systems for new quantum applications [6], since they only suffer from loss as decoherence mechanism and current development of low-loss equipment enables a new generation of experiment. Crucial for both applications and fundamental questions, in the optical domain, is the ability to generate large photonic states in well-defined optical modes [7], as well as detecting them with sufficient efficiency. Starting with the landmark experiment by Hanbury-Brown and Twiss [8], the statistical properties of photons have been used in a broad range of contexts to observe and exploit nonclassical effects.

Two-mode squeezed states with large photon numbers can be considered macroscopic [9] as they exhibit a large Fisher information [10]. Using the process of parametric down-conversion (PDC), bright squeezed states with billions of photons have been demonstrated [11–17]. However, the multimode nature of this approach frequently impairs the direct comparison between theoretical predictions and experimental observations and limits the applications of these states. In particular, further processing with non-Gaussian measurements projects multimode states into mixed states, thereby diminishing significantly the quantum character. On the contrary, the combination of photon-number measurements with genuine single- or two-mode squeezed vacuum states has been shown to overcome Gaussian no-go theorems [18], to enable continuous-variable entanglement distillation [19,20] and to allow for the preparation of cat states [21,22]. Recent developments in transition edge sensors (TES) [23] and nanowire detectors [24] offer the possibility to perform photon-number measurements with single-photon resolution and very high efficiency.

Tight filtering [25] or mode selection [26] could be used to reduce the number of modes, at a cost of reducing the size of the systems and achievable purity due to unavoidable losses [27]. In the single-photon regime pulsed PDC sources with tailored dispersion properties have been developed, which are capable of directly generating PDC states in one mode only [28,29]. Such single-mode PDC states have been shown experimentally at the single-photon level using bulk PDC [30] and up to a mean photon number of 2.5 using a waveguide [31]. When increasing the pump power further, detrimental effects might be introduced, such as time ordering effects [27,32], self-phase modulation [33], and photorefractive damage [34,35], which may degrade the mode structure.

In this Letter, we demonstrate that an engineered PDC source remains single mode for a broad range of pump energies and allows nonclassical, non-Gaussian states of up to 50 photons to be heralded in single modes. Using superconducting TES, we perform photon-number measurements and show nonclassical phenomena in the photon statistics with photon numbers spanning a space of dimension $80 \times 80$. We measure the full photon-number distribution of the state, which allows us to analyze correlation functions up to 40th order, demonstrate joint photon-number squeezing with unprecedented measurement resolution, and show negative parity in the raw data.

Source design and implementation.—We use type II PDC, where signal and idler photons are orthogonally polarized and ideally described by a product of two-mode squeezed vacuum states:

$$ |\psi\rangle = \bigotimes_k \sqrt{1 - \lambda_k^2} \sum_n \lambda_k^n |n\rangle_k, $$

(1)
where \( k \) labels frequency modes, \( n \) is the photon number in each mode, and \( \lambda = \tanh(\tau) \). The squeezing parameter \( \tau \) scales linearly with the pump field amplitude, the nonlinear coefficient \( \chi^{(2)} \), the interaction length inside the crystal, and the mode overlap of the pump and PDC modes. Having perfect photon-number correlations, the PDC states can be used to herald Fock states—states with well-defined photon number.

Spectrally single-mode operation, i.e., \( \lambda_k = 0 \) for \( k > 1 \), can be achieved by engineering the momentum conservation (phase matching) condition of the nonlinear interaction [28], which typically means engineering the nonlinear dielectric medium and pump properties. Spatial correlations can be fully suppressed by using a waveguide, which is single mode for the signal and idler down-converted modes. Such single-mode generation of PDC in a waveguide has been demonstrated in Ref. [31], yet the brightness of the source has not been explored.

Typical approaches to generate single-mode PDC states use bulk crystals. To generate bright states in a bulk nonlinear medium, the pump must be tightly focused to achieve a large nonlinear interaction, which, at very high pump powers, may introduce higher-order nonlinear effects. A waveguide geometry has the benefit of increasing the process efficiency in a single spatial mode by 2 orders of magnitude compared to bulk PDC sources, due to confinement of the pump beam [36].

A schematic of our experimental setup is shown in Fig. 1. In the single-photon regime, the periodically poled KTP (ppKTP) waveguide source has shown single-photon purities above 80% [37]. The nonlinear medium consists of an 8 mm long ppKTP waveguide engineered to produce decorrelated and degenerate signal and idler modes at 1535 nm. The chip has been commercially purchased from ADVR. We pump the chip with 1 ps optical pulses containing energies of up to 2.5 nJ and producing states with a mean photon number of up to 80 photons. For pump pulse energies up to 1.5 nJ, we measure the photon numbers, shot to shot, with TES [23]. The TES have a near unity detection efficiency and feature single-photon resolution below 20 photons at 1535 nm but can detect up to 100 photons with a few-photon uncertainty [38]. We analyze the TES response for each event based on trace overlaps with calibration traces from known coherent state inputs (see Supplemental Material [39] for further details). We use either one TES on each mode for states with mean photon numbers \( \langle n \rangle < 10 \) or two TES on each mode for one state with \( \langle n \rangle = 20 \). Additionally, we use an avalanche photodiode (APD) with calibrated attenuators to measure mean photon numbers up to 80.

Results.—The measured photon-number probabilities, shown in Fig. 2(a) for the state \( \langle n \rangle = 20 \), feature photon-number correlations as well as a logarithmic decaying diagonal, as expected from Eq. (1) with only one spectral mode. The vacuum component is still the highest element despite measured mean photon numbers of 11 and 9 in each mode. This directly reveals the single-mode character of the

**FIG. 1.** Setup. Transform-limited pulsed light from a Ti:sapphire laser is spectrally filtered to produce 1 ps pulses and coupled into the periodically poled KTP waveguide (WG). A long pass (LP) filter removes the pump after the down-conversion process in the waveguide and a band pass (BP) filter suppresses the sinc sidelobes of the phase matching function. Signal and idler are split at a polarizing beam splitter (PBS), coupled into single-mode fibers and connected to (up to four) transition edge sensors (TES).

**FIG. 2.** (a) Raw photon-number correlation matrix of the state \( \langle n \rangle = 20 \) with exponentially decaying diagonal elements (inset, logarithmic scale). (b) Mean photon number in one mode versus pump power measured with a low efficiency APD. The excellent fit with only one fit parameter \( \alpha \) indicates that the state stays single mode up to at least 80 photons. (c) Noise reduction factor (NRF) for different mean photon numbers, showing the non-classical correlations in the state. Statistical error bars in (b) and (c) are smaller than the data points.
state; for a multimode state, the mixture of different thermal distributions would tend towards a Poissonian distribution as the number of modes increases. To quantify the single-modeness, we calculate the second-order autocorrelation function \[ g^{(2)}(0) = \langle n^2 \rangle - \langle n \rangle^2 / \langle n \rangle^2, \] where \( n \) is the photon number, on the marginal distribution of each mode. For thermal statistics, \( g^{(2)}(0) = 2 \), and for Poissonian statistics, \( g^{(2)}(0) = 1 \). For the state shown in Fig. 2(a) we obtain 1.89(3) and 1.87(3) for signal and idler, respectively. This corresponds to effective mode numbers \( K = 1/(|g^{(2)}(0) - 1|) \) of 1.12(4) and 1.15(4), where 1 would be the ideal case. All uncertainties given in this Letter correspond to the 1s standard deviation. We see no dependence of the effective mode number on pump power.

When we use the highest pump powers available to us, the source generates states with a mean photon number of 80, corresponding to \( r = 2.9(\lambda = 0.99) \). The mean photon numbers as a function of pump power follow the expected curve for this measurement up to the highest available powers; see Fig. 2(b). For this single measurement, we use an APD, calibrated using the Klyshko method [50].

The nonclassicality of our state can be seen directly in the raw data. Any classical state, by definition, can be written as a mixture of coherent states with a positive probability distribution. Hence, the photon-number uncertainty of \( \sqrt{N} \) in a pulse with a mean photon number of \( N \) imposes a lower bound on the antidiagonal width \( n_s - n_i \) in Fig. 2(a). To encapsulate this criterion, one figure of merit is the noise reduction factor [12], \( \text{NRF} = \text{Var}(n_s - n_i)/\langle n_s + n_i \rangle \), which is necessarily \( \geq 1 \) for classical states. For ideal PDC with a detection efficiency of \( \eta \), the NRF is equal to \( 1 - \eta \). We measure values below 0.4, see Fig. 2(c), in those cases where we use one TES on each mode, in agreement with the measured efficiencies of around 66%. This corresponds to 4.2 dB of correlated photon-number squeezing not corrected for losses. In the case where we use two TES on each mode, the NRF is higher due to slightly lower and more asymmetric efficiencies in that configuration.

The nonclassicality can also be seen in heralded states. For one- and three-photon heralded states, we see negative parities \( \langle (-1)^n \rangle \) of \(-0.131(1)\) and \(-0.013(2)\) in the raw heralded data, which is a sufficient condition for nonclassicality. For higher heralded states, the parity tends to zero and is obscured by statistical errors.

A more robust criterion is the heralded \( g^{(2)}(0) \) value, i.e., the \( g^{(2)}(0) \) in one mode conditioned on a certain outcome in the other mode. For ideal \( n \)-photon Fock states, \( g^{(2)}(0) = 1 - 1/n \). Values below 1 indicate nonclassical sub-Poissonian statistics. Even heralding on a 50-photon event, the measured states fulfill this nonclassicality criterion; see Fig. 3. With increasing photon number, the transition from strongly nonclassical states to classical states becomes apparent as they become harder to distinguish. Producing larger nonclassical states would require reducing the losses in the heralding mode. At the current efficiencies, the 50 photon event happens about twice per second with a PDC mean photon number of 7.

Having access to the full photon-number distribution allows us to go beyond the well-established second-order \( g^{(2)}(0) \) and calculate a higher-order correlation function which may be defined by \[ g^{(m,n)} = \langle a^\dagger a^n a^\dagger a^m \rangle / \langle a^\dagger a \rangle^n \] for one mode and \[ g^{(m,m,n)} = \langle a^\dagger a^m b^\dagger b^m b^\dagger b^n \rangle / \langle a^\dagger a \rangle^m \langle b^\dagger b \rangle^n \] for two modes, where \( a, a^\dagger \) and \( b, b^\dagger \) are the usual annihilation and creation operators. In Fig. 4 we show the results of both cases. The measured values are in excellent agreement with the theoretical predictions. Further details on correlation functions are given in the Supplemental Material [39].

The excellent agreement with theory indicates that the limiting factor is indeed the loss in our setup. We calculate our system efficiencies by either assuming perfect photon-number correlations [51] or by a least-squares fit (see Supplemental Material [39]). We obtain 60% and 64% for signal and idler, respectively, using the first method and 64% and 68% using the second method, with systematic uncertainties around 3%. The efficiencies are slightly higher in the latter case because we allow for Poissonian and thermal noise in the original data stemming from either an optical background or a nonperfect photon-number resolution in the detectors. Such noise behaves like loss in the first method. For the \( \langle n \rangle = 20 \) state, the second method gives 43% and 52% for signal and idler. Here, the efficiencies are lower due to the change of the experimental configuration from two TES to four TES requiring an extra pair of fiber beam splitters.

Total efficiencies close to 70% are among the highest in the literature [52–55]. These high efficiencies are the reason why we see clear nonclassical features in the raw data without loss inversion. For example, negative parity can only be observed above 50% in principle.
Given the performance of the source, we can estimate the potential continuous-variable squeezing [47] achievable with the current setup. In the literature, to our knowledge, the highest squeezing directly measured in a single pass, pulsed system is 5 dB [56] and in a continuous-wave cavity system 12.7 dB [57]. In our source, the maximum mean photon number of 80 would correspond to 25 dB of squeezing. The measurable squeezing, however, would be limited by the current efficiencies to about 4.5 dB.

The main loss contributions in the setup come from the coupling to single-mode fibers of around 80% and the linear optical elements with a total transmission of about 90%. With on-chip integration of polarizing beam splitters and detectors, of which both have been demonstrated [58,59], the total efficiencies could go up to above 90%. With on-chip integration of polarizing beam splitters and detectors, of which both have been demonstrated [58,59], the total efficiencies could go up to above 90%. This would push the size of possible nonclassical states to hundreds of photons. The ultimate goal would be an efficiency around 99%, at which fault tolerant quantum computation with continuous-variable cluster states becomes possible [60].

Conclusion.—Observing nonclassical correlations of photons is fundamental to quantum optics. We have shown that these correlations persist with the largest number of photons to date in a single-mode state. The single-mode nature of these states allows us to herald large photon-number states in a controlled and efficient way. When combined with non-Gaussian projective measurements and homodyne detection, a broad range of continuous-variable experiments in the strongly squeezed, pulsed regime become possible.

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G. H. and T. J. B. contributed equally to this work.

*georg.harder@uni-paderborn.de
