

light source and monitored the central wavelength λ_C with an optical spectrum analyzer (OSA). The beam was strongly attenuated to yield on average less than one photon per pulse before being coupled into a *DK-40* DCF module from Lucent. The photons were then detected by an *id201* InGaAs APD from id-Quantique with a measured temporal jitter of only $\sigma_{\tau, \text{APD}} = 180$ ps. We recorded the time difference $\Delta\tau$ between the electronic laser trigger and the electronic response from the APD with a time-to-digital converter (TDC) for a set of three different spectra with $\lambda_C = 1531, 1484,$ and 1391 nm, and observed corresponding peaks at $\Delta\tau = 1874, 1884,$ and 1990 ns. Utilizing the TDC, we were able to quantify $\Delta\tau$ with a precision of 81 ps.

By relating the peaks from the OSA spectrum with the temporal peaks from the time measurement (see Fig. 2) we obtained a calibration curve (inset) for reconstructing the entire set of spectra. A least-squares polynomial fit relating the arrival time τ to the monitored wavelength was used as the calibration curve $c(\tau)$. It is clearly evident from Fig. 2(c) that the spectral width and shape of the OSA measurement overlap well with the reconstructed spectra. Although the input pulse is strongly attenuated, the DCF measurements show much better SNR, and the side lobe of the darkest colored curve is much more pronounced, indicating an excellent resolution.

Furthermore, we investigated the capabilities, potential limitations, and experimental constraints encountered when using our setup for recovering a spectrum. The derivative of the quadratic fit function gives a GVD between -0.11 ns/nm at 1325 nm and -0.25 ns/nm at 1575 nm. With a detection jitter of $\sigma_{\tau, \text{APD}} = 180$ ps, a resolution of 0.72 nm can be achieved at 1550 nm. Resolution can be increased using a longer fiber at the cost of higher losses and greater expense. The fit for the calibration function $c(\tau)$ to three calibration wavelengths is an approximation that may give rise to systematic errors. We estimate these errors to be of magnitude ± 0.1 nm at ≈ 1520 nm and ± 0.5 nm at ≈ 1550 nm. This uncertainty poses no principal restriction and can be reduced by using more reference spectra for the cali-

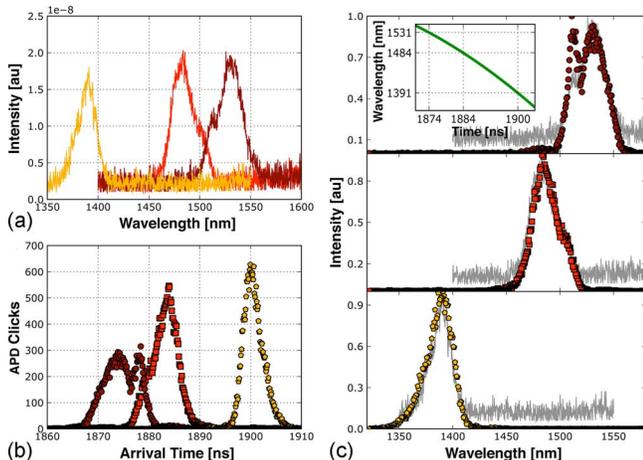


Fig. 2. (Color online) Calibration using three reference spectra: (a) OSA reference spectrum, (b) arrival time $\Delta\tau$, (c) comparison of original and reconstructed spectra.

bration. If the laser repetition rate is above a certain threshold it is possible that several light pulses are present simultaneously in the DCF. This will cause problems for the reconstruction only if the spectrum of a pulse is so broad that it becomes mixed with the following pulse. We avoided this problem by reducing the 80 MHz repetition rate of our laser down to 1 MHz with a pulse picker. We determined the travel time through the fiber to be $16.6 \mu\text{s}$, or equivalently a fiber length of 3.3 km. In addition, APDs exhibit a wavelength-dependent variation of the single-photon detection probability $p_D(\lambda)$. Hence, it is crucial to renormalize the recorded click histogram against the detection probability $p_D(\lambda)$ if the wavelength range under observation is too large for $p_D(\lambda)$ to be assumed flat.

After having ensured a reliable reconstruction of single-photon spectra we employed our scheme to measure the spectrum of a PDC source. Our setup for this application of the spectrograph is shown in Fig. 3(a) and allowed us to analyze the marginal as well as joint correlation spectrum of the PDC. We pumped an 18-mm-long periodically poled potassium titanyl phosphate waveguide with a $4 \mu\text{m} \times 4 \mu\text{m}$ cross section and generated a wave function of two photons as

$$|\Psi\rangle = \int d\omega_s d\omega_i F(\omega_s, \omega_i) a^\dagger(\omega_s) b^\dagger(\omega_i) |0, 0\rangle$$

with a spectral amplitude function $F(\omega_s, \omega_i)$. Our goal was to analyze precisely the biphotonic correlation properties of the spectral intensity distribution $|F(\omega_s, \omega_i)|^2$.

The PDC process was pumped by an ultrafast pulsed Ti:Sa laser system at 765 nm with FWHM of 1.9 nm to produce photon pairs at 1544 nm and 1517 nm in a Type II process, such that signal and

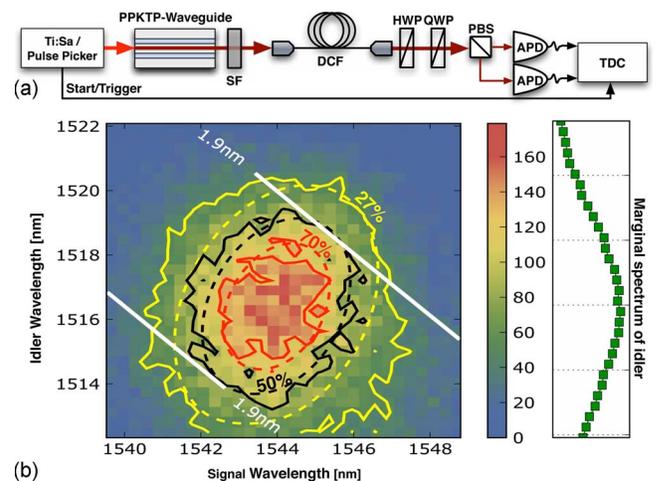


Fig. 3. (Color online) (a) Experimental setup for measuring marginal and joint correlation spectra of a PDC source (see text). Not shown is the programmable delay generator used for gating the APDs. (b) Measured correlation spectrum between signal and idler corresponds to the joint spectral intensity $|F(\omega_s, \omega_i)|^2$. A white line marks the 1.9 nm FWHM of the pump envelope. Solid and dashed contour lines are shown for theory and experiment, respectively.

idler photons emerged from the waveguide with orthogonal linear polarization. Both photons were coupled into the DCF with 25% efficiency. Since the fiber was not polarization-preserving, signal and idler photons carried elliptic, but still orthogonal, polarization states at the fiber output. To restore their linear polarization we applied a quarter- and a half-waveplate. Finally, a PBS split the signal and the idler, and they were guided to *id201* InGaAs APDs.

As the polarization rotation caused by the DCF was wavelength dependent we could not perfectly reconstruct the original linear polarization and thus unambiguously split signal and idler photons for their entire spectrum. Nevertheless, we were able to achieve a reasonable polarization contrast of 80% for both signal and idler beams. Since signal and idler were not degenerate in wavelength, we could identify and discard the photons that took the “wrong” path at the PBS by their arrival time, and thus the quality of our measured spectra were not degraded. In principle, all polarization-related problems would be avoided by separating signal and idler immediately after the waveguide. This, however, would require two DCFs.

In the telecommunication wavelength regime, because of the small semiconductor bandgap, current APDs need to be operated in a gated mode to suppress dark counts and afterpulsing. We thus scanned the time domain by electronically delaying the laser trigger in steps of 100 ps. We selected the shortest possible gate width such that all detection events occurred in a $\sigma_{\tau, \text{APD}} \approx 200$ ps window. The delay was independently varied for signal and idler. Each coincident detection event yielded a pair of arrival times that could be mapped to wavelengths with the measured calibration curve via $(\lambda_s, \lambda_i) = [c(\tau_s), c(\tau_i)]$.

The calibration curve $\lambda = c(\tau + \delta\tau)$ is unique up to an offset $\delta\tau$ that is introduced when the spectrometer is used in a setting where the optical path length differs from that of the calibration setup. We derived this offset by taking into account energy conservation $1/\lambda_p = 1/\lambda_s + 1/\lambda_i = 1/c(\tau_s + \delta\tau) + 1/c(\tau_i + \delta\tau)$ of the PDC process. With this offset we were able to reconstruct both the marginal and the coincidence spectrum of our PDC source with high precision, as shown in Fig. 3(b).

In summary, we have introduced a technique for measuring directly the spectrum of ultrafast pulses at the single-photon level using GVD in a highly dispersive fiber. We showed how to calibrate and apply such an apparatus for measurements at wavelengths of ≈ 1550 nm with both high resolution and high SNR. Thereafter, we enhanced our scheme to measure two-dimensional coincidence spectra, and thus demonstrated a characterization of the joint spectral intensity of signal and idler photons from a PDC source at telecommunication wavelengths. Our approach might become even more attractive for cur-

rent experiments performed at 800 nm as this offers the advantage of making full use of the DCF as a spectrograph, since no gating is required by visible-light-sensitive Si-APDs. Because of the simplicity and accuracy of our experimental setup we expect the DCF spectrograph to become a versatile tool for the characterization of optical quantum states.

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